- 4. [9 points] The city of Rainneapolis has a strange weather pattern. It is always sunny, except for February 2nd, when it rains substantially all day. This year, Amin prepared for the stormy day by building a machine which continuously removes rainwater from his backyard.
  - Let T(h) be the **total amount** of rainwater in Amin's backyard, in cubic feet, h hours after 12:00am on February 2nd.
  - Let A(h) be the **rate** at which the rain **adds** water to Amin's backyard, in cubic feet per hour, h hours after 12:00am on February 2nd.
  - Let M(h) be the **rate** at which Amin's **machine removes** rainwater from his backyard, in cubic feet per hour, h hours after 12:00am on February 2nd.

The functions T(h), A(h), and M(h) are all differentiable. Assume that there is **no rainwater** in Amin's backyard **before** it starts raining at 12:00am on February 2nd.

- **a**. [3 points] Which of the following gives a correct interpretation of  $\int_{4}^{10} M(h) dh = 8000$ ? Circle **all** correct answers.
  - (i) The total amount of rainwater in Amin's backyard decreases by 8000 cubic feet from 4:00am to 10:00am on February 2nd.
  - (ii) Between 4:00am and 10:00am on February 2nd, Amin's machine removes a total of 8000 cubic feet of rainwater from his backyard.
  - (iii) The rate at which Amin's machine removes rainwater from his backyard between 4:00am and 10:00am on February 2nd is 8000 cubic feet per hour.
  - (iv) At 10:00am on February 2nd, Amin's machine removes rainwater from his backyard at a rate of 8000 cubic feet per hour faster than at 4:00am.
  - (v) NONE OF THESE
- **b**. [3 points] Which of the following expressions gives the **total amount** of rainwater, in cubic feet, in Amin's backyard at 7:00am? Circle **all** correct answers.

(i) 
$$\int_0^7 T'(h) dh$$
 (ii)  $\int_0^7 T(h) dh$  (iii)  $\int_0^7 (A(h) + M(h)) dh$   
(iv)  $\int_0^7 A(h) dh - \int_0^7 M(h) dh$  (v) NONE OF THESE

c. [3 points] Which of the following expressions gives the **average amount** of rainwater, in cubic feet, in Amin's backyard between 6:00am and 9:00am? Circle **all** correct answers.

(i) 
$$\frac{1}{9-6} \int_{6}^{9} T'(h) dh$$
 (ii)  $\frac{1}{9-6} \int_{6}^{9} T(h) dh$  (iii)  $\frac{T(9) - T(6)}{9-6}$   
(iv)  $\frac{1}{3} \int_{0}^{9} T(h) dh + \frac{1}{3} \int_{6}^{0} T(h) dh$  (v) NONE OF THESE

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