

4. (15 points) Circle “True” or “False” for each of the following statements. Circle “True” only if the statement is always true. No explanation is necessary.

(a) If  $\lim_{n \rightarrow \infty} a_n = 0$ , then  $\sum_{n=0}^{\infty} a_n$  converges.

True.  False.

(b) If  $0 \leq a_n \leq b_n$  for all  $n$ , and if  $\sum_{n=1}^{\infty} a_n$  diverges, then  $\sum_{n=1}^{\infty} b_n$  diverges.

True.  False.

(c) If  $P_4(x) = 5 + 6(x - a) + 2(x - a)^2 + 37(x - a)^3 + 21(x - a)^4$  is the 4th degree Taylor polynomial for  $f(x)$  about  $x = a$ , then  $f^{(3)}(a) = 37$ .

True.  False.

(d) If the power series  $\sum_{n=0}^{\infty} C_n(x - 3)^n$  converges for  $x = 1$ , then it also converges for  $x = 4$ .

True.  False.

(e) The infinite series  $\sum_{n=1}^{\infty} \frac{3n^2+n}{n^5+3}$  converges.

True.  False.

5. (5 points) Express the number  $x$  whose repeating decimal expansion is  $6.17636363636363\dots$  as the sum of an infinite series.

$$\begin{aligned} 6.17636363636363\overline{63} &= 6.17 + \frac{63}{10,000} + \frac{63}{1,000,000} + \frac{63}{100,000,000} + \dots \\ &= 6.17 + 63 \sum_{n=2}^{\infty} \frac{1}{100^n} \\ &= 6.17 + \frac{63}{100} \sum_{n=1}^{\infty} \frac{1}{100^n}. \end{aligned}$$