

1. (12 points) Let  $f(x) = 2e^{x/2}$ .

(a) (4 pts.) Find  $P_2(x)$ , the Taylor polynomial for  $f(x)$  of degree 2 centered at  $x = 1$ .

(b) (3 pts.) Graph the functions  $f(x)$  and  $P_2(x)$  for  $0 \leq x \leq 2$  on the same set of axes. Label each function clearly.

(c) (2 pts.) Use the polynomial  $P_2(x)$  that you wrote in part (a) to estimate  $f(0.1)$  and  $f(1.1)$ .

(d) (3 pts.) Briefly demonstrate which of the previous two approximations is more accurate.