

5. [14 points] A particle moves on the unit circle according to the parametric equations

$$x(t) = -\sin(bt^2) \quad , \quad y(t) = \cos(bt^2) \quad \text{and } b > 0.$$

for  $0 \leq t \leq \pi$ . Make sure to show all your work.

- a. [1 point] What is the starting point of the particle?
- b. [2 points] In which direction (counterclockwise/clockwise) is the particle moving along the circle? Justify.
- c. [5 points] Find an expression for the speed of the particle. Simplify it as much as possible.
- d. [2 points] At what value of  $t$  in  $[0, \pi]$  is the speed of the particle the largest?
- e. [4 points] Find the equation of the tangent line to the parametric equation at  $t = \sqrt{\frac{\pi}{3b}}$ .