6. [8 points] Members of the recruitment committee for the Mars University (MU) chapter of the fraternity Epsilon Rho Rho are designing a pledge pin to distribute during Rush Week. The pin takes the shape of a cardioid with a circular hole in it. The cardioid is given by a polar equation of the form $r_{1}=a+b \cos (\theta)$, while the circular hole has the polar equation $r_{2}=\cos (\theta)$. The pin is pictured below, where the $x$ - and $y$-axes are measured in inches.

a. [5 points] The committee plans on coating one side of the pin in gold plating, which costs 3 dollars per square inch. Give an expression representing the cost to plate one face of the pin in gold. Your answer may involve integrals and the constants $a$ and $b$.
b. [3 points] Find $a$ and $b$.

$$
a=
$$

$$
b=
$$

$\qquad$

