

1. [12 points] Determine if the following integrals converge or diverge. If the integral converges, circle the word “converges” and give the **exact value** (i.e. no decimal approximations). If the integral diverges, circle “diverges”. In either case, **you must show all your work and indicate any theorems you use**. Any direct evaluation of integrals must be done **without using a calculator**.

a. [6 points]  $\int_0^1 \frac{e^x \sin(2x) - (2e^x - 2) \cos(2x)}{\sin^2(2x)} dx$

$\left( \text{Note: } \frac{d}{dx} \left( \frac{e^x - 1}{\sin(2x)} \right) = \frac{e^x \sin(2x) - (2e^x - 2) \cos(2x)}{\sin^2(2x)} \right)$

Converges

Diverges

b. [6 points]  $\int_2^\infty \frac{1}{(\ln x)^2 x} dx$

Converges

Diverges