

8. [9 points] Boxer Paul “Stretch” Cassenick decides to do some footwork training by practicing moving around the boxing ring. The ring is in the shape of a 20x20 foot square, and Paul’s movement is modeled by the differential equation

$$\frac{dy}{dx} = f(x, y),$$

for some function  $f(x, y)$ . The following table gives some values of  $f(x, y)$ .

$x \backslash y$	0	5	10	15	20
0	3	1	1	0	-2
5	0	0	0	0	0
10	2	1	2	0	2
15	0	-1	-3	0	1
20	-2	0	-2	0	-3

- a. [6 points] If  $y(0) = 0$ , use Euler’s method with  $\Delta x = 5$  to estimate  $y(20)$ . You must show your calculation for each step of Euler’s method to receive full credit.

- b. [3 points] Circle all of the following that **could** be equilibrium solutions.

$x = 5$

$x = 15$

$y = 5$

$y = 15$