

2. [9 points] Note: “Closed form” here means that the expression should NOT include sigma notation or ellipses (...) and should NOT be recursive.

In the live-action series adaptation of *Derivative Girl*, Derivative Girl can lift $D_0 = 1000$ kg, and she can make as many copies of herself as she wants. The first copy can lift $1/3$ the amount Derivative Girl can lift, and the n th copy can lift $1/3$ the amount the $(n - 1)$ st copy can lift.

- a. [3 points] Let D_n be the amount of mass, in kg, that the n th copy of Derivative Girl can lift. Calculate D_1 and D_2 , and give a closed-form expression for D_n in terms of n :

$$D_1 = \underline{\hspace{2cm}}$$

$$D_2 = \underline{\hspace{2cm}}$$

$$D_n = \underline{\hspace{2cm}}$$

- b. [4 points] Let G_n be the amount of mass, in kg, that Derivative Girl and the first n copies can lift together. Calculate G_1 and G_2 , and give a closed-form expression for G_n :

$$G_1 = \underline{\hspace{2cm}}$$

$$G_2 = \underline{\hspace{2cm}}$$

$$G_n = \underline{\hspace{2cm}}$$

- c. [2 points] If Derivative Girl could make infinitely many copies, what is the largest amount, in kg, that Derivative Girl and her copies could lift together? Your answer should be a closed-form expression.

Answer: $\underline{\hspace{2cm}}$