

4. [8 points] The amount of time it takes a spider to build a web is  $t$  hours. The **cumulative distribution function** for  $t$  is given by:

$$J(t) = \begin{cases} 0, & \text{for } t \leq \frac{1}{2} \\ \frac{16}{9} \left( -\frac{1}{3}t^3 + \frac{5}{4}t^2 - t + \frac{11}{48} \right), & \text{for } \frac{1}{2} < t < 2 \\ 1, & \text{for } 2 \leq t \end{cases}$$

- a. [2 points] What appears to be the shortest amount of time it could take the spider to build a web? Include units.

**Answer:** \_\_\_\_\_

- b. [2 points] What is the probability that it will take the spider more than 1 hour to build a web?

**Answer:** \_\_\_\_\_

- c. [4 points] Write an expression for the mean amount of time it takes the spider to build a web. Your answer may involve one or more integrals, but should not involve the letter  $J$ .

**Answer:** \_\_\_\_\_