

**2.** [15 points]

**a.** [9 points] For each of the following sequences, defined for  $n \geq 1$ , state clearly whether the sequence is:

- increasing, decreasing, or neither.
- bounded or unbounded.
- convergent or divergent.

No justification is needed.

(i)  $a_n = 2 - \cos(\pi n)$

(ii)  $b_n = \int_1^{n^2} \frac{1}{x} dx$

(iii)  $c_n = 13 - \sum_{k=0}^n \frac{1}{(1.1)^k}$

**b.** [6 points] Let  $\sum_{n=1}^{\infty} d_n$  be a geometric series, with  $d_2 = 16$  and  $d_5 = 2$ . Determine, and clearly state, whether the series converges or diverges. If the series converges, find its sum.