

6. [11 points] It's fall, and the leaves are falling onto the grass. Over the course of each day, suppose that 10kg of leaves fall onto the grass. At the beginning of each day, 50 percent of the leaves currently on the grass (from previous days) are removed.
- a. [3 points] Let  $M_n$  be the total mass in kg of all the leaves currently on the grass at the **end** of the  $n$ th day. Suppose that  $M_1 = 10$ . Write expressions for  $M_2$  and  $M_3$ . The letter  $M$  should not appear in your answer.
- b. [5 points] Find a closed-form expression for  $M_n$ . This means that your answer should be a function of  $n$ , should not contain  $\Sigma$ , and should not be recursive.
- c. [3 points] If 30kg of leaves are on the grass at the end of any day, then the grass will die. Will this happen during the fall? Justify your answer.