

2. [7 points] Let $f(x)$ and $g(x)$ be two continuous and differentiable functions on $[1, \infty)$. Further, suppose these functions have the following properties:

- $F(x) = \frac{g(x)}{x + \ln(x)}$ is an antiderivative of $f(x)$ for $x \geq 1$,
- $g(1) = 11$,
- $\lim_{x \rightarrow \infty} g(x) = \infty$,
- $\lim_{x \rightarrow \infty} g'(x) = 21$.

Compute the value of the following improper integral if it converges. if it does not converge, use a **direct computation** of the integral to show its divergence. Be sure to show your full computation, and be sure to use **proper notation**.

$$\int_1^{\infty} f(x) dx$$

Circle one: **Diverges** **Converges to** _____