

3. [8 points]

a. [5 points] Show that the following limit converges and compute the limit. Fully justify your answer including using **proper limit notation**.

$$\lim_{n \rightarrow \infty} n^2 \left(1 - \cos \left(\frac{1}{n} \right) \right)$$

Answer: _____

b. [3 points] Use part a. to determine if the following series converges or diverges, and circle the corresponding word. **Fully justify** your answer including using **proper notation** and showing mechanics of any tests you use.

$$\sum_{n=1}^{\infty} n^2 \left(1 - \cos \left(\frac{1}{n} \right) \right)$$

Circle one:

Converges

Diverges

Justification: