

4. (8 points) Show that if  $\sum_{n=1}^{\infty} a_n$  converges, then  $\lim_{n \rightarrow \infty} a_n = 0$ .

5. (8 points) In this question we will investigate the convergence of the power series  $\sum_{n=0}^{\infty} \frac{n^2}{e^n} (x + 2)^n$ .

(a) Find the radius of convergence,  $R$ , of the power series. (Show your work.)

$R =$  \_\_\_\_\_.

(b) What is the interval of convergence of the power series?

\_\_\_\_\_  $< x <$  \_\_\_\_\_.