

9. [14 points] An ice cube melts at a rate proportional to its surface area. Let  $V(t)$  denote the volume (in  $\text{cm}^3$ ) of the ice cube, and let  $x(t)$  denote the length (in cm) of a side of the ice cube  $t$  seconds after it begins to melt.
- a. [4 points] Write a differential equation for  $V(t)$ , the ice cube's volume  $t$  seconds after it started melting. Your differential equation may contain  $V$ ,  $t$  and an unknown constant  $k$ .
- b. [4 points] The ice cube's initial volume is  $V_0 > 0$ . Solve the differential equation you found in part (a), finding  $V$  in terms of  $t$ ,  $k$ , and  $V_0$ .
- c. [6 points] Graph the volume of the ice cube versus time given  $V(0) = V_0$ . Be sure to label your axes and any important features of your graph, including the time at which the ice cube has completely melted.