

1. [16 points] Carla and Bobby run a race after spinning in circles for a good amount of time to make themselves dizzy. They start at the origin in the  $xy$ -plane and they race to the line  $y = 5$ . Assume the units of  $x$  and  $y$  are meters.

Bobby's position in the  $xy$ -plane  $t$  seconds after the race starts is

$$\left(-\sqrt{3}t \cos t, \frac{1}{\sqrt{3}}t \sin t\right)$$

and Carla's position in the  $xy$ -plane  $t$  seconds after the race starts is

$$(t \sin t, -t \cos t).$$

- a. [4 points] Write an integral that gives the distance that Carla travels during the first two seconds of the race. Do not evaluate your integral.

- b. [3 points] Find Carla's speed at  $t = \pi$ .

Carla's speed at  $t = \pi$  is \_\_\_\_\_

- c. [4 points] Carla and Bobby are so dizzy that they run into each other at least once during the race. Find the first time  $t > 0$  that they run into each other, and give the point  $(x, y)$  where the collision occurs.

They first run into each other at  $t =$  \_\_\_\_\_

The collision occurs at  $(x, y) =$  \_\_\_\_\_

- d. [5 points] Bobby's phone flies out of his pocket at  $t = \pi/2$ . It travels in a straight line in the same direction as he was moving at  $t = \pi/2$ . Find the equation of this line in Cartesian coordinates.

The equation for the line is \_\_\_\_\_