7. [16 points] A treasure hunter has spotted a large exotic rock at the bottom of a deep pit. The vertical distance from the top of the pit to the top of the rock is 15 meters. To retrieve the rock, the treasure hunter attaches a 15 meter rope to the top of the rock and lifts it out of the pit. The rope used has mass 2 kg per meter. Below, do not simplify your final answers or evaluate any integrals. As a reminder, the acceleration due to gravity is $g$, where $g=9.8 \mathrm{~m} / \mathrm{s}^{2}$.
a. [8 points] If the rock has mass 4 kg , write an expression involving integrals for the amount of work, in Joules, the treasure hunter does in lifting the rock and the attached rope 10 meters up from the bottom of the pit.
Hint: Once rope has been raised to the top of the pit, the treasure hunter no longer needs to lift it.


#### Abstract

Answer: $\qquad$ b. [8 points] After the rock has been lifted 10 meters off the bottom of the pit, the rock starts to crumble, losing 0.1 kg of mass per second. The treasure hunter resumes lifting the rock at a constant speed of 0.5 meters per second. Write an expression involving integrals for the amount of work, in Joules, the treasure hunter does in lifting the crumbling rock (and the attached rope) the remaining 5 meters to the top of the pit.


 The hint from part a. still applies.
## Answer:

$\qquad$

