

4. [11 points] Zach is playing the retro video game *Plaque-Man* all day to get a new personal high score. Zach starts playing the game with 0 points. Over the course of each hour, Zach scores an additional 2500 points. At the **beginning** of every hour, Zach trades 20% of his points to buy extra time. For  $n \geq 1$ , let  $H_n$  be Zach's score at the **end** of the  $n$ th hour of playing the game.

For example,  $H_1 = 2500$ .

- a. [4 points] Write expressions for  $H_2$  and  $H_3$ . Your answers should not involve the letter  $H$ . You do not need to simplify your expressions.

$$H_2 = \underline{\hspace{15em}}$$

$$H_3 = \underline{\hspace{15em}}$$

- b. [4 points] Write a **closed-form** expression for  $H_n$ . *Closed-form* means your answer should not include ellipses (...) or sigma notation ( $\Sigma$ ), and should not be recursive. You do not need to simplify your closed-form expression.

**Answer:**  $H_n = \underline{\hspace{15em}}$

- c. [3 points] Find Zach's eventual score if he keeps playing *Plaque-Man* indefinitely. You do not need to simplify your numerical answer.

**Answer:**  $\underline{\hspace{15em}}$