7. (5 points) For  $-\frac{\sqrt{\pi}}{2} \le x \le \frac{\sqrt{\pi}}{2}$ , let A(x) be the area of the region bounded by the curves  $\cos(t^2)$ ,  $\sin(t^2)$ , and the vertical lines  $t = -\frac{\sqrt{\pi}}{2}$  and t = x. See the figure below.



(a) Sketch on the figure an area that represents  $\Delta A = A(x + \Delta x) - A(x)$  for a small number  $\Delta x$ .

(b) Find a formula for the derivative A'(x).

## **ANSWER** : A'(x) = \_\_\_\_\_.

8. (6 points) For what values of the positive number p does the infinite series  $\sum_{n=1}^{\infty} \frac{n^3 - 4n^2}{n^p + 5}$  converge? Explain the reason for your answer.