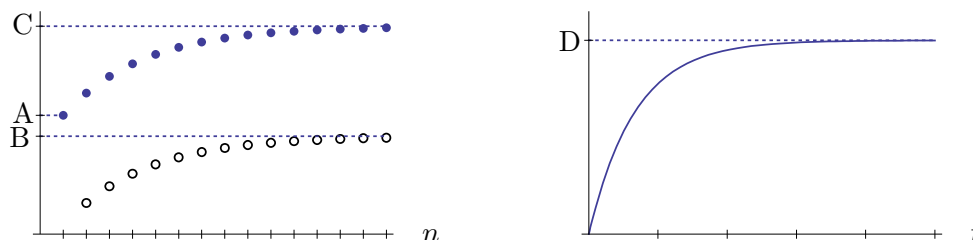


- c. [4 points] This is the third part of problem (6), which begins on the previous page. The figure below shows graphs that may correspond to the solutions that you obtained in (6a) and (6b). The graph to the left corresponds to part (a), with the solid and open circles in the graph showing the amount of ibuprofen in the patient after and before the  $n$ th pill. The graph to the right corresponds to (b). Assuming that these graphs do represent your solutions, use your results from (a) and (b) to determine the values of A, B, C, and D.



7. [16 points] The annual snowfall in Ann Arbor has mean 52.91 inches and standard deviation 12.67 inches. Assume that these data are normally distributed, and let  $x$  be the deviation of a year's snowfall from the mean (so that if  $x = -2$  in a given year, it means that the snowfall that year was 50.91 inches). Then the probability density function for  $x$  is

$$p(x) = \frac{1}{\sigma\sqrt{2\pi}} e^{-x^2/(2\sigma^2)} = 0.03149 e^{-x^2/321.1},$$

so that its cumulative distribution function  $P(x)$  is

$$P(x) = \int_{-\infty}^x p(t) dt = \int_{-\infty}^x 0.03149 e^{-t^2/321.1} dt.$$

- a. [2 points] Explain why  $P(x) = \frac{1}{2} + \int_0^x 0.03149 e^{-t^2/321.1} dt$ .

This continues problem 7: here,  $p(x) = 0.03149 e^{-x^2/321.1}$ , and

$$P(x) = \frac{1}{2} + \int_0^x 0.03149 e^{-t^2/321.1} dt.$$

- b. [5 points] Write a Taylor series for  $p(x)$  (around  $x = 0$ ).
- c. [5 points] Write a Taylor series for  $P(x)$  (around  $x = 0$ ). *Hint: you will probably want to use your work from (b).*
- d. [4 points] Use your result from (b) or (c) to estimate the probability that there will be up to 60 inches of snow this winter.