9. [15 points] The graph shows the area between the graphs of $f(x) = 6\cos(\sqrt{2x})$ and $g(x) = x^2 + x$. Let (x_0, y_0) be the intersection point between the graphs of f(x) and g(x).



- **a**. [6 points] Compute P(x), the function containing the first three nonzero terms of the Taylor series about x = 0 of $f(x) = 6\cos(\sqrt{2x})$.
- **b.** [3 points] Use P(x) to approximate the value of x_0 .
- c. [3 points] Use P(x) and the value of x_0 you computed in the previous question to write an integral that approximates the value of the shaded area. Find the value of this integral.

- **d**. [1 point] Graph f(x) and g(x) in your calculator. Use the graphs to find an approximate value for x_0 .
- e. [2 points] Write a definite integral in terms of f(x) and g(x) that represents the value of the shaded area. Find its value using your calculator.