

3. [12 points] Let

$$I = \int_0^1 \left(1 + \frac{t^2}{2}\right)^{\frac{5}{2}} dt$$

- a. [5 points] Approximate the value of  $I$  using Right(2) and Mid(2). Write each term in your sums.
- b. [2 points] Are your estimates of the value of  $I$  obtained using Right(2) and Mid(2) guaranteed to be overestimates, underestimates or neither?
- c. [3 points] Find the first three nonzero terms of the Taylor series for  $g(t) = \left(1 + \frac{t^2}{2}\right)^{\frac{5}{2}}$  about  $t = 0$ .
- d. [2 points] Use your answer from part (c) to estimate  $I$ .