

6. [12 points] In the following problems, support all your answers by stating the test(s) or facts you used to prove convergence or divergence. Show all your work.

a. [4 points]  $\sum_{n=1}^{\infty} \frac{\sqrt{n}}{1+n^3}$       Circle your answer:      Converges      Diverges

b. [4 points]  $\sum_{n=1}^{\infty} \frac{1}{2 + \cos^2(n)}$       Circle your answer:      Converges      Diverges

- c. [4 points] For which values of  $a$  does the series

$$\sum_{n=1}^{\infty} \frac{a^n}{3^n} = \frac{a}{3} + \frac{a^2}{9} + \frac{a^3}{27} + \cdots$$

converge? For the values of  $a$  where the series converges, find the sum of the series.