7. [14 points] You want to open a savings account to deposit 1000 dollars. Three banks offer the following options:

   a. [3 points] Bank A offers its clients a savings account that earns 1.5% per year compounded annually. Define the sequence $A_n$ to be the amount of money in the savings account $n$ years after you deposit your 1000 dollars. Find a formula for $A_n$.

   b. [7 points] Bank B offers its clients a savings account that earns 2% per year compounded annually. At the end of each year, after the bank deposits the interest you earned, it withdraws a 1 dollar service fee from the account. Define the sequence $B_n$ to be the amount of money, right after the service fee deduction, in the savings account $n$ years after you deposit your 1000 dollars. Find $B_1$, $B_2$, $B_3$ and a closed form formula for $B_n$.

   c. [4 points] Bank C offers its clients a savings account that earns interest continuously at a rate of 1.5% of the current balance per year. At the same time, the bank withdraws a service fee from the account at a rate of 1 dollar per year continuously. Let $M(t)$ be the amount of money in the savings account $t$ years after you deposit your 1000 dollars. Write the differential equation satisfied by $M(t)$. Include initial conditions.