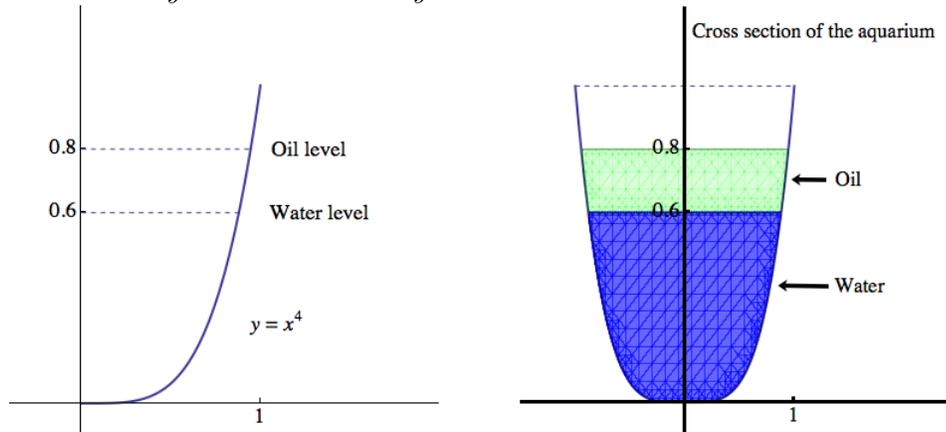


9. [13 points] Olive oil has been poured into the Math Department's starfish aquarium! The shape of the aquarium is a solid of revolution, obtained by rotating the graph of $y = x^4$ for $0 \leq x \leq 1$ around the y -axis. Here x and y are measured in meters.



The aquarium contains water up to a level of $y = 0.6$ meters. There is a layer of oil of thickness 0.2 meters floating on top of the water. The water and olive oil have densities 1000 and 800 kg per m^3 , respectively. Use the value of $g = 9.8$ m per s^2 for the acceleration due to gravity.

- a. [6 points] Give an expression involving definite integrals that computes the total mass of the water in the aquarium.
- b. [7 points] Give an expression involving definite integrals that computes the work necessary to pump all the olive oil to the top of the aquarium.