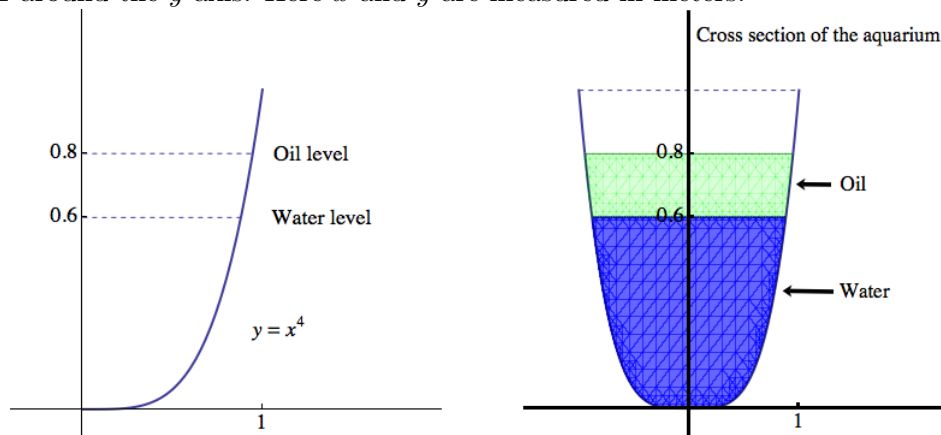


9. [13 points] Olive oil has been poured into the Math Department's starfish aquarium! The shape of the aquarium is a solid of revolution, obtained by rotating the graph of  $y = x^4$  for  $0 \leq x \leq 1$  around the  $y$ -axis. Here  $x$  and  $y$  are measured in meters.



The aquarium contains water up to a level of  $y = 0.6$  meters. There is a layer of oil of thickness 0.2 meters floating on top of the water. The water and olive oil have densities 1000 and 800 kg per  $\text{m}^3$ , respectively. Use the value of  $g = 9.8$  m per  $\text{s}^2$  for the acceleration due to gravity.

- a. [6 points] Give an expression involving definite integrals that computes the total mass of the water in the aquarium.

- b. [7 points] Give an expression involving definite integrals that computes the work necessary to pump all the olive oil to the top of the aquarium.