

7. [14 points] Chickens continue to appear around you, and Franklin's army is hesitant to advance.
- a. [6 points] Let  $F(t)$  give the total number of chickens that have arrived after  $t$  seconds. You observe that  $F(t)$  obeys the following differential equation

$$\frac{dF}{dt} = e^{-F} t^2.$$

If there are initially 20 chickens, find a formula (in terms of  $t$ ) for  $F(t)$ .

- b. [4 points] A large, familiar-looking chicken steps forward from the flock and clucks, "Koo Koo Katcha!". This large chicken waddles towards Franklin following the parametric equations

$$x(t) = \frac{\sin(\pi t) + 1}{\pi} \qquad y(t) = \ln(t + 1)$$

where  $t$  is the time, in seconds, after the chicken steps forward from the flock and both  $x$  and  $y$  are measured in feet. Find the chicken's speed 10 seconds after it steps forward. Include units.

- c. [4 points] Franklin says, "BEEP BOOP BEEP. YOU'RE RIGHT, WHAT HAVE I BECOME?" A single robot tear falls from Franklin's robot eye. Consider the region in the  $xy$ -plane bounded by  $y = \frac{\sin(x)}{x + 2}$ ,  $x = \pi$ ,  $x = 2\pi$ , and the  $x$ -axis. The volume of Franklin's tear is given by rotating this region around the  $x$ -axis. Write an integral giving the volume of Franklin's tear. Do not evaluate this integral.