

1. [4 points] Suppose that the power series $\sum_{n=0}^{\infty} c_n(x-3)^n$ converges at $x = 6$ and diverges at $x = -2$. What can you say about the behavior of the power series at the following values of x ? For each part, circle the correct answer. Ambiguous responses will be marked incorrect.

a. [1 point] At $x = -3$, the power series...

CONVERGES

DIVERGES

CANNOT DETERMINE

b. [1 point] At $x = 0$, the power series...

CONVERGES

DIVERGES

CANNOT DETERMINE

c. [1 point] At $x = 8$, the power series...

CONVERGES

DIVERGES

CANNOT DETERMINE

d. [1 point] At $x = 2$, the power series...

CONVERGES

DIVERGES

CANNOT DETERMINE

2. [5 points] Determine the **radius** of convergence of the power series

$$\sum_{n=0}^{\infty} \frac{(2n)!}{(n!)^2} x^{2n}.$$

Justify your work carefully and write your final answer in the space provided. Limit syntax will be enforced.

Radius of convergence = _____