

8. [11 points] In this problem, we consider the parametric curve given by

$$x = f(t) \qquad y = g(t)$$

for all  $t$ , where  $f$  and  $g$  are twice-differentiable functions. Some values of  $f$  and  $g$  and their derivatives are given in the tables below.

$t$	1	2	3	4	5
$f(t)$	-3	-4	-3	-1	1
$g(t)$	5	2	-2	-4	-1

$t$	1	2	3	4	5
$f'(t)$	-2	0	1	3	1
$g'(t)$	-4	-2	-1	0	2

- a. [1 point] In the space provided, write an integral that gives the arc length of the parametric curve from  $t = 1$  to  $t = 5$ .

Arc length = \_\_\_\_\_

- b. [3 points] Use a midpoint sum with as many subdivisions as possible to estimate your integral from part a. Write out all the terms in your sum, and do **not** simplify.

- c. [3 points] Find the Cartesian equation for the tangent line to the parametric curve in the  $xy$ -plane at  $t = 1$ .

- d. [2 points] Consider the tangent lines to the parametric curve at the  $t$ -values  $t = 1, 2, 3, 4, 5$ . Are any of these lines **perpendicular** to each other? If so, list any **two**  $t$ -values for which the tangent lines are perpendicular. If not, write "NO."

- e. [2 points] As  $t$  ranges from 1 to 5, the corresponding part of the parametric curve intersects the line  $y = x$  exactly once. Which interval contains the  $t$ -value for which the curve intersects the line  $y = x$ ? Circle your answer. You do not need to show any work.

(1, 2)

(2, 3)

(3, 4)

(4, 5)