9. [12 points] Read the following parts carefully, and circle the appropriate answer(s). Some parts may have more than one correct answer.

6

a. [3 points] Circle the value(s) of x for which the following identity holds:

$$2 = x^{3} + \frac{x^{6}}{2!} + \frac{x^{9}}{3!} + \frac{x^{12}}{4!} + \cdots$$

$$\sqrt[3]{\ln(2)} \qquad \qquad \boxed{\sqrt[3]{\ln(3)}} \qquad \qquad (\ln(2))^{3}$$

$$e^{2^{3}} \qquad \qquad \ln(\sqrt[3]{3}) \qquad \qquad e^{\sqrt[3]{3}}$$

a

b. [3 points] Raymond Green's pet anaconda Sheela grew 5 m in length over the past month. The veterinarian says that each month, the increase in Sheela's length will be 40% of the increase the month before. How much longer (in meters) will Sheela be one year from now? Circle **all** that apply.

$$\sum_{k=0}^{12} 5(0.4)^k \qquad \boxed{\frac{2(1-(0.4)^{12})}{1-0.4}} \qquad \boxed{\sum_{k=1}^{12} 5(0.4)^k}$$
$$\frac{5(1-(0.4)^{12})}{1-0.4} \qquad \frac{2(1-(0.4)^{13})}{1-0.4}$$

c. [3 points] Let $\alpha > 0$ be a constant. What is the value of the convergent series $\sum_{n=1}^{\infty} \frac{(-1)^{n+1} \alpha^n}{(2n)!}$?

 $\cos(\alpha) - 1$ $\cos(\sqrt{\alpha}) - 1$ $1 - \cos(\alpha)$

$$\alpha - \cos(\sqrt{\alpha})$$
 $1 - \cos(\sqrt{\alpha})$ $\cos(\alpha) - \alpha$

d. [3 points] Which of the following series converge absolutely? Circle all that apply.

$$\frac{\sum_{n=1}^{\infty} \frac{\sin^{99}(n)}{n^2}}{\sum_{n=2}^{\infty} \frac{(-1)^{n+1}}{\ln(n)}} \sum_{n=2}^{\infty} \frac{8^n + (-1)^n 10^n}{9^n}$$

$$\frac{\sum_{n=2}^{\infty} \frac{(-1)^{n+1}}{n(\ln(n))^{1.01}}}{\sum_{n=2}^{\infty} \frac{(-1)^n}{n}}$$