

7. [11 points] Some values of a function  $m(x)$  and its derivatives are given below.

$x$	0	2
$m(x)$	4	1
$m'(x)$	-1	0
$m''(x)$	0	0
$m'''(x)$	3	-2
$m''''(x)$	5	8

- a. [4 points] Find a formula for  $P_4(x)$ , the Taylor polynomial of degree 4 for  $m(x)$  about  $x = 2$ .

**Answer:**  $P_4(x) =$  \_\_\_\_\_

- b. [3 points] Use your answer to approximate the value of  $\int_1^3 m(x) dx$ . Show your work.

**Answer:**  $\int_1^3 m(x) dx \approx$  \_\_\_\_\_

- c. [4 points] Let  $G(x)$  be the antiderivative of the function  $g(x) = m(3x^2)$  with  $G(0) = 5$ . Find the first three nonzero terms of the Taylor series for  $G(x)$  about  $x = 0$ .

**Answer:** \_\_\_\_\_