

2. [5 points] Suppose that the power series $\sum_{n=1}^{\infty} C_n(x+2)^n$ converges at $x = 4$ and diverges at $x = -10$. What can you say about the behavior of the power series at the following values of x ?

a. [1 point] At $x = 0$, the power series...

CONVERGES DIVERGES CANNOT DETERMINE

b. [1 point] At $x = -8$, the power series...

CONVERGES DIVERGES CANNOT DETERMINE

c. [1 point] At $x = 8$, the power series...

CONVERGES DIVERGES CANNOT DETERMINE

d. [1 point] At $x = -4$, the power series...

CONVERGES DIVERGES CANNOT DETERMINE

e. [1 point] At $x = 6$, the power series...

CONVERGES DIVERGES CANNOT DETERMINE

3. [7 points] A function $F(x)$ has Taylor series given by

$$F(x) = \sum_{n=0}^{\infty} \frac{(-1)^n(n+1)}{2^n(n^2+1)}(x-1)^{4n+1}$$

Answer the following questions regarding the Taylor series:

- a. [3 points] Circle the appropriate answer. No work is needed, but partial credit may be given for correct work.

At $x = 1$, F is... INCREASING DECREASING CANNOT DETERMINE

- b. [4 points] What is $F^{(2021)}(1)$? Give your answer in exact form and do not try to simplify. Show your work.

$$F^{(2021)}(1) = \underline{\hspace{10cm}}.$$