7. [17 points] John is holding a Fan Fair to celebrate the success of his burgeoning fan business. At the fair, John is debuting his new fan, which has blades given by the shaded region of the graph of the polar equation $r=\cos (3 \theta)+\frac{1}{2}$ shown below. Note that the graph of $r=\cos (3 \theta)+\frac{1}{2}$ is comprised of both the inner and outer loops of the fan blades. One of the activities at the Fan Fair is to guess the perimeter and area of the blades, which can actually be computed explicitly.

a. [4 points] For the values of $\theta$ listed below, write on the line the letter of the point corresponding to it.

$$
\begin{array}{ll}
\theta=0: \quad & \theta=\frac{\pi}{3}: \\
\theta=\frac{\pi}{2}: \quad & \theta=\pi:
\end{array}
$$

b. [5 points] Find the 3 values of $\theta$ which correspond to the point $C$ (the origin) for $0 \leq \theta \leq \pi$. Then, determine the interval within $[0,2 \pi]$ for which $\theta$ traces out the dashed loops in the graph above. (Hint: $\cos \frac{2 \pi}{3}=\cos \frac{4 \pi}{3}=-\frac{1}{2}$ )
$\theta=$ $\qquad$
Interval giving $\theta$-values that trace out the dashed loops: $\qquad$
7. (continued) Here is a reproduction of the graph from the previous page of the polar equation $r=\cos (3 \theta)+\frac{1}{2}$ :

c. [4 points] Write, but do not evaluate, an expression involving one or more integrals that gives the total perimeter of the fan blades, including both the inner and outer edges of the fan blades.

Total Perimeter $=$ $\qquad$
d. [4 points] Write, but do not evaluate, an expression giving the total area of all 3 fan blades (the shaded region of the graph). (Hint: Your answer from (b) may be handy, but is not strictly necessary)
$\qquad$

