- 8. [9 points] Gabriella is developing a new kind of vuvuzela. In order to come up with a new method, she first considers the old way she made her instruments.
  - a. [4 points] Gabriella initially made her vuvuzelas by considering a positive function f(x), and forming a region  $\mathcal{R}$  between y = f(x) and the x-axis on the interval  $[2, \infty)$ . She rotated  $\mathcal{R}$  about the x-axis to form the shape of the vuvuzela. Write an integral which gives the volume of the vuvuzela. Your answer will involve the function f(x).

Answer:

**b.** [5 points] For her new batch of vuvuzelas, Gabriella considers an entirely different shape. The volume of the new design of vuvuzela is given by

$$\int_2^\infty \frac{x}{(x^2+5)^2} \, \mathrm{d}x.$$

Compute the value of this integral if it converges. If it does not converge, use a **direct** computation of the integral to show its divergence. Be sure to show your full computation, and be sure to use **proper notation**.

Circle one: Diverges Converges to \_\_\_\_\_