9. [8 points] A power series centered at $x=3$ given by

$$
\sum_{n=0}^{\infty} \frac{n^{2}+1}{2^{n}(n+2)}(x-3)^{n} .
$$

The radius of convergence of this power series is 2 (do NOT show this). Find the interval of convergence of this power series. Show all your work, including full justification for series behavior.

