

1. [12 points] Compute the exact value of each of the following, if possible. Your answers should not involve integration signs, ellipses or sigma notation. For any values which do not exist, write **DNE**. You do not need to show work.

a. [2 points] The integral $\int_{-10}^{10} (f(x) + 1) dx$, where $f(x)$ is an odd function.

Answer: 20

b. [2 points] The integral $\int_{-3}^4 \frac{1}{x^4} dx$.

Answer: DNE

c. [2 points] The sum $\sum_{n=0}^{2023} 7(5)^n$.

Answer: $\frac{7(1 - 5^{2024})}{1 - 5} = \frac{7}{4}(5^{2024} - 1)$

- d. [2 points] The **radius of convergence** for the Taylor series centered around $x = 0$ for the function $g(x) = (1 + 3x^2)^{1/5}$.

Answer: $\frac{1}{\sqrt{3}}$

e. [2 points] The infinite sum $(0.5)^2 - \frac{(0.5)^4}{2} + \frac{(0.5)^6}{3} - \dots + \frac{(-1)^{n+1}(0.5)^{2n}}{n} + \dots$.

Answer: $\ln\left(\frac{5}{4}\right)$

- f. [2 points] The value of $h''(2)$ where the fourth-degree Taylor polynomial for $h(x)$ about $x = 2$ is given by $P_4(x) = 2 + 9(x - 2) - 81(x - 2)^4$.

Answer: 0