

3. [13 points] In this week's snail race there are three snail competitors: snails A, B and C. All three snails start at the left wall of an aquarium (located at $x = 0$), and must cross the tank to the right-hand wall (located at $x = 100$). The paths of snails A and B are given below. All three snails start at $t = 0$, and stop when they reach the right-hand wall of the aquarium. The time t is measured in seconds, and all distances are in millimeters.

$$\begin{aligned} \text{A: } x(t) &= 10t, & y(t) &= \frac{t^2}{3} \\ \text{B: } x(t) &= t^2 - 7t + 82, & y(t) &= -\frac{t^3}{4} + 250 \end{aligned}$$

- a. [3 points] When do snails A and B finish the race? Which of these two snails reaches the finish line first?

Answer: Snail A finishes at $t =$ _____ seconds.

Answer: Snail B finishes at $t =$ _____ seconds.

Answer: The winner of these snails is snail _____.

- b. [4 points] Write an expression using one or more integrals for the distance that snail A travels during the race. Do not evaluate any integrals in your expression.

Answer: Snail A travels _____ mm.

- c. [3 points] Snail C travels in a straight line from the origin through the point $(40, 30)$. Which, if any, of the following could be a parametric equation describing snail C's *path* (disregarding speed) during the race? Circle **all** options which apply.

i. $x(t) = 40t, \quad y(t) = 30t$

iv. $x(t) = 30 \sin t, \quad y(t) = 40 \sin t$

ii. $x(t) = 30t, \quad y(t) = 40t$

v. $x(t) = 40 \sin(t + \frac{\pi}{2}), \quad y(t) = 30 \sin(t + \frac{\pi}{2})$

iii. $x(t) = \sin t, \quad y(t) = \frac{3}{4} \sin t$

vi. NONE OF THE ABOVE

- d. [3 points] Now assume that snail C travels at a constant speed of 10mm/s, still in a straight line from the origin through the point $(40, 30)$. Which, if any, of the following could be a parametric equation describing snail C's *motion* (including speed) during the race? Circle **all** options which apply.

i. $x(t) = 8t, \quad y(t) = 6t$

iv. $x(t) = 40 \sin t, \quad y(t) = 30 \sin t$

ii. $x(t) = 40t, \quad y(t) = 30t$

v. $x(t) = 10 \sin t, \quad y(t) = 10 \cos t$

iii. $x(t) = 8 \sin t, \quad y(t) = 6 \sin t$

vi. NONE OF THE ABOVE