

6. [10 points] Consider the function  $f(x) = \ln(1+x)$  and its Taylor series about  $x = 0$ .
- a. [4 points] Determine the first four non-zero terms of the Taylor series for  $f(x) = \ln(1+x)$  about  $x = 0$ . Be sure to show enough work to support your answer.

- b. [4 points] Find the first three non-zero terms of the Taylor series for  $g(x) = \ln\left(\frac{1+x}{1-x}\right)$  about  $x = 0$ . Be sure to show enough work to support your answer. (*Hint: You may find it helpful to utilize properties of logarithms.*)

- c. [2 points] Find the exact value of the sum of the series

$$2\left(\frac{3}{4}\right) + \frac{2}{3}\left(\frac{3}{4}\right)^3 + \frac{2}{5}\left(\frac{3}{4}\right)^5 + \dots$$