

4. [8 points] You are trapped on an island, and decide to build a signal fire to alert passing ships. You start the fire with 200 pounds of wood. During the course of a day, 40% of the wood pile burns away (so 60% remains). At the end of each day, you add another 200 pounds of wood to the pile. Let W_i denote the weight of the wood pile immediately after adding the i^{th} load of wood (the initial 200-pound pile counts as the first load).
- a. [3 points] Find expressions for W_1 , W_2 and W_3 .
- b. [3 points] Find a closed form expression for W_n (*a closed form expression* means that your answer should not contain a large summation).
- c. [2 points] Instead of starting with 200 pounds of wood and adding 200 pounds every day, you decide to start with P pounds of wood and add P pounds every day. If you plan to continue the fire indefinitely, determine the largest value of P for which the weight of the wood pile will never exceed 1000 pounds.