

2. [13 points] Determine if each of the following sequences is increasing, decreasing or neither, and whether it converges or diverges. Circle all the answers that apply. On parts **a-c**, if the sequence converges, find the limit. No justification is required.

a. [3 points] For  $n \geq 1$ , let  $a_n = 3 + \frac{1}{n}$ .

b. [3 points] For  $n \geq 1$ , let  $a_n = \left(-\frac{\pi}{e}\right)^n$ .

c. [3 points] Let  $P(x)$  be the cumulative distribution function of a nonzero probability density function  $p(x)$ . Define  $a_n = P(n)$  for  $n \geq 1$ .

d. [2 points] For  $n \geq 1$ , let  $a_n = 1 - \frac{1}{1!} + \frac{1}{2!} - \frac{1}{3!} + \cdots + \frac{(-1)^n}{n!}$ .

e. [2 points] Let  $a_n = \int_2^n \frac{1}{\sqrt{x}-1} dx$ , for  $n \geq 2$ .