

3. [10 points] A boat's initial value is \$100,000; it loses 15% of its value each year. The boat's maintenance cost is \$500 the first year and increases by 10% annually. In the following questions, your formulas should not be recursive.

- a. [2 points] Let B_n be the value of the boat n years after it was purchased. Find B_1 and B_2 .

Solution:

$$B_1 = \$100,000(0.85).$$

$$B_2 = \$100,000(0.85)^2.$$

- b. [3 points] Find a formula for B_n .

Solution: $B_n = 100,000(.85)^n$

- c. [2 points] Let M_n be the total amount of money spent on the maintenance of the boat during the first n years. Find M_2 and M_3 .

Solution:

$$M_2 = 500(1 + 1.1)$$

$$M_3 = 500(1 + 1.1 + (1.1)^2)$$

- d. [3 points] Find a closed form formula for M_n .

Solution: $M_n = 500 \frac{(1 - (1.1)^n)}{1 - 1.1}$