

5. [10 points] Compute the **exact value** of each of the following. You do not need to show work.

a. [2 points] Find the radius of convergence  $R$  of  $\sum_{n=1}^{\infty} \frac{5(x-1)^n}{3^n}$ .

**Answer:**  $R =$  \_\_\_\_\_

b. [2 points]  $\sum_{n=1}^{100} e^n$

**Answer:**  $\sum_{n=1}^{100} e^n =$  \_\_\_\_\_

c. [2 points]  $\lim_{n \rightarrow \infty} \int_{-\infty}^n p(t) dt$ , where  $p(t)$  is a probability density function.

**Answer:**  $\lim_{n \rightarrow \infty} \int_{-\infty}^n p(t) dt =$  \_\_\_\_\_

d. [2 points] Find the function  $f(x)$  satisfying  $\int x^3 e^x dx = x^3 e^x - \int f(x) dx$

**Answer:**  $f(x) =$  \_\_\_\_\_

e. [2 points]  $\sum_{n=0}^{\infty} \frac{(-4)^n}{(2n)!}$

**Answer:**  $\sum_{n=0}^{\infty} \frac{(-4)^n}{(2n)!} =$  \_\_\_\_\_