

7. [6 points] The function  $r(t)$ , defined for all real numbers  $t$ , gives the position of a particle moving along the unit circle, where

$$r(t) = (\cos(t - t^3), \sin(t - t^3)).$$

- a. [3 points] Find all values of  $t$  where the particle stops moving.

**Answer:**  $t =$  \_\_\_\_\_

- b. [3 points] For which values of  $t$  is the particle moving counterclockwise?

**Answer:** \_\_\_\_\_

8. [8 points] Let  $f(x) = xe^{-x^2}$ .

- a. [4 points] Find the first four nonzero terms of the Taylor series for  $f(x)$  centered at  $x = 0$ .

**Answer:** \_\_\_\_\_

- b. [2 points] Find the value of  $f^{(18)}(0)$ .

**Answer:**  $f^{(18)}(0) =$  \_\_\_\_\_

- c. [2 points] Compute the limit

$$\lim_{x \rightarrow 0} \frac{xe^{-x^2} - x}{5x^3}.$$

**Answer:**  $\lim_{x \rightarrow 0} \frac{xe^{-x^2} - x}{5x^3} =$  \_\_\_\_\_