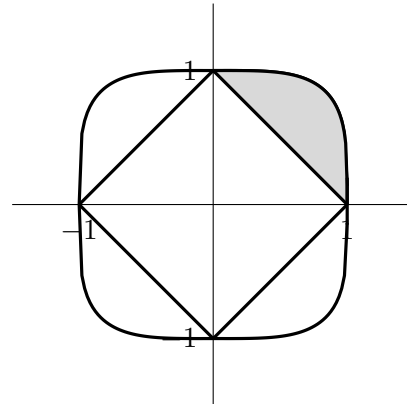


2. [8 points]

The *castar*, a coin widely used in Middle-Earth, allegedly has the shape graphed to the right. The outer perimeter can be modeled by the implicit equation

$$x^4 + y^4 = 1$$

and the perimeter of the hole in the middle is a square. To help his fellow Hobbits detect counterfeit coins, Samwise Gamgee, the Mayor of the Shire, is working on obtaining the specifications of a genuine castar. Sam needs your help.



- a. [2 points] Find a function  $f(\theta)$  so that the outer edge of the castar is given by the function  $r = f(\theta)$ .

**Answer:**  $f(\theta) =$  \_\_\_\_\_

- b. [3 points] Write an expression involving one or more integrals that gives the total area of the quarter of a castar in the first quadrant (shaded above).

**Answer:** \_\_\_\_\_

- c. [3 points] Approximate the area of a castar by estimating your integral(s) from part (b) using TRAP(2). Write out all the terms in your sum(s).

**Answer:** \_\_\_\_\_