

5. [12 points] A large four-leaf clover, pictured below, resides in a forest.

- The leaves of the clover are modeled by the polar curve

$$r = 2 \sin(2\theta)$$

for $0 \leq \theta \leq 2\pi$. This is the **solid** curve in the diagram to the right.

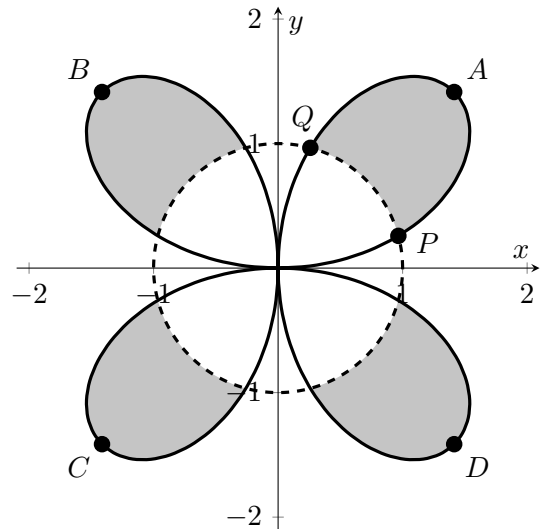
- The polar curve

$$r = 1$$

for $0 \leq \theta \leq 2\pi$ is the **dashed** curve in the diagram to the right.

The leaves of the clover are light green inside of this curve, and dark green outside of it.

- All distances are measured in inches.



- a. [2 points] Which of the following points labelled in the diagram above is in the portion of the polar curve $r = 2 \sin(2\theta)$ traced out for $\frac{\pi}{2} \leq \theta \leq \pi$? Circle the **one** correct answer. No justification is required.

Circle one: A B C D NONE OF THESE

- b. [5 points] The points P and Q , labelled above, are two intersection points of the solid and dashed curves. Write P and Q in **polar coordinates** (r, θ) , where $r \geq 0$ and $0 \leq \theta \leq 2\pi$. Please show all of your work.

Answer: $P: (r, \theta) =$ _____ $Q: (r, \theta) =$ _____

- c. [5 points] Write an expression involving **at most two integrals** that gives the **area**, in square inches, of the dark green part of the four-leaf clover. (This is the shaded region in the diagram above.) **Do not evaluate your integral(s).**

Answer: _____