7. [10 points] Consider the function

$$g(x) = \frac{1}{3}\cos(x^2) - x\sin(x)$$

a. [5 points] Give the first three non-zero terms of the Taylor series of g(x) centered about x = 0. Show all your work.

Answer:

b. [5 points] The function g(x) has a continuous antiderivative, G(x), with a Taylor series that converges for all x. Given that G(0) = 8, find the first four non-zero terms of the Taylor series for G(x) centered about x = 0. Show all your work.