

3. [15 points] Consider the equation  $y' = ay - y^4$ .
- a. [5 points] Find all critical points for this equation.
- b. [6 points] Draw a phase line for each of the cases  $a = -2, 0, 2$ . Determine the stability of the critical points in each case.
- c. [4 points] Sketch a *bifurcation diagram* that shows the position of the critical points as a function of  $a$  in the  $ay$ -plane.