4. (a) (4 points) Solve the initial-value problem $x^{\prime}=x^{2} / t+3 x^{2} t^{2}, x(-1)=\frac{1}{2}$, for $x=x(t)$.

(b) (4 points) A general solution of the differential equation $x^{\prime}=t / x$ for $x=x(t)$ has the implicit form $x^{2}-t^{2}=C$. Find the (maximal) interval of existence of the solution with initial condition $x(5)=4$.

