

3. [14 points] Use Laplace transforms to solve each of the following.

a. [7 points]  $y'' + 4y' + 4y = 2e^{-2t}$ ,  $y(0) = 1$ ,  $y'(0) = 0$ .

b. [7 points]  $y'' + 3y' = \begin{cases} 12, & 0 \leq t < 2 \\ 0, & t \geq 2 \end{cases}$ ,  $y(0) = 0$ ,  $y'(0) = 0$ .