1. [12 points] Six matrices and their eigenvalues and eigenvectors are given below. Use this information to answer the questions below. Be sure that you explain your answers.

| $\mathbf{A}_{1}$ | $\mathbf{A}_{2}$ | $\mathbf{A}_{3}$ | $\mathbf{A}_{4}$ | $\mathbf{A}_{5}$ | $\mathbf{A}_{6}$ |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\left(\begin{array}{cc}-1 & 2 \\ -1 & -3\end{array}\right)$ | $\left(\begin{array}{ll}2 & 2 \\ 1 & 3\end{array}\right)$ | $\left(\begin{array}{cc}-2 & 2 \\ 1 & -3\end{array}\right)$ | $\left(\begin{array}{cc}-1 & 3 \\ 2 & -2\end{array}\right)$ | $\left(\begin{array}{ll}-2 & -2 \\ -1 & -3\end{array}\right)$ | $\left(\begin{array}{cc}-3 & -1 \\ 1 & -1\end{array}\right)$ |
| $\lambda_{1,2}=-2 \pm i$ | $\lambda_{1,2}=1,4$ | $\lambda_{1,2}=-4,-1$ | $\lambda_{1,2}=-4,1$ | $\lambda_{1,2}=-4,-1$ | $\lambda_{1,2}=-2,-2$ |
| $\mathbf{v}_{1}=\binom{2}{-1+i}$ | $\mathbf{v}_{1}=\binom{-2}{1}$ | $\mathbf{v}_{1}=\binom{-1}{1}$ | $\mathbf{v}_{1}=\binom{-1}{1}$ | $\mathbf{v}_{1}=\binom{1}{1}$ | $\mathbf{v}_{1}=\binom{-1}{1}$ |
| $\mathbf{v}_{2}=\binom{2}{-1-i}$ | $\mathbf{v}_{2}=\binom{1}{1}$ | $\mathbf{v}_{2}=\binom{2}{1}$ | $\mathbf{v}_{2}=\binom{3}{2}$ | $\mathbf{v}_{2}=\binom{-2}{1}$ | $\mathbf{w}=\binom{1}{0}$ |

a. [6 points] Write a linear system involving one of the $\mathbf{A}_{j}$ that could have the phase portrait shown to the right.

b. [6 points] Write a linear system involving one of the $\mathbf{A}_{j}$ that could have the phase portrait shown to the right.


